Math 2001. Counting Problems
(permutations and combinations)
(1) How many lists of lengths 3 can be made from the symbols A, B, C, D, E, F if $\ldots$ (a) ...repetition is allowed?
(b) ... repetition is not allowed?
(c) ... repetition is allowed and the list must start with the letter A?
(d) ... repetition is not allowed and the list must not start with the letter A?
(e) ... repetition is allowed and the list must contain the letter A?
(f) ...repetition is not allowed and the list must contain the letter A?
(2) Consider lists made from the symbols A, B, C, D, E, with repetition allowed.
(a) How many such length-4 lists have at least one letter repeated?
(b) How many such length-4 lists contain exactly two different letters?
(c) How many such length- 5 lists have at least one letter repeated?
(d) How many such length- 5 lists contain exactly two different letters?
(e) How many such length-6 lists have at least one letter repeated?
(f) How many such length-5 lists are there if the letters A, B, C must appear consecutively in the list?
(g) How many such length-6 lists are there if the letters A, B, C must appear consecutively in the list?
(h) How many such length-5 lists are there if the list must start with a vowel, end with a vowel, and use all the five letters?

