MATH 2001. COUNTING PROBLEMS (permutations and combinations)

- (1) How many lists of lengths 3 can be made from the symbols A, B, C, D, E, F if ...
 - (a) ... repetition is allowed?
 - (b) ... repetition is not allowed?
 - (c) ... repetition is allowed and the list must start with the letter A?
 - (d) ... repetition is not allowed and the list must not start with the letter A?
 - (e) ... repetition is allowed and the list must contain the letter A?
 - (f) \dots repetition is not allowed and the list must contain the letter A?

- (2) Consider lists made from the symbols A, B, C, D, E, with repetition allowed.(a) How many such length-4 lists have at least one letter repeated?
 - (b) How many such length-4 lists contain exactly two different letters?
 - (c) How many such length-5 lists have at least one letter repeated?
 - (d) How many such length-5 lists contain exactly two different letters?
 - (e) How many such length-6 lists have at least one letter repeated?
 - (f) How many such length-5 lists are there if the letters A, B, C must appear consecutively in the list?
 - (g) How many such length-6 lists are there if the letters A, B, C must appear consecutively in the list?
 - (h) How many such length-5 lists are there if the list must start with a vowel, end with a vowel, and use all the five letters?