

MATH 4140. HOMEWORK 3  
Due Wednesday, February 10

**Note:** All numbered exercises are from Erdmann–Holm ([EH]).

- (1) Read Sections 2.1–2.3 of [EH].
- (2) Exercise 1.22. (In Part (b), assume that the algebra  $A$  is finite dimensional.)
- (3) Exercise 2.1.
- (4) Prove the statements in Example 2.13.(6).
- (5) Exercise 2.10.
- (6) Exercise 2.21.(a)–(b).
- (7) Prove that the ideal generated by the elements  $x, y$  is not principal in the algebra  $k[x, y]$  (so  $k[x, y]$  is not a PID).
- (8) Show that a left ideal of a  $k$ -algebra is automatically a  $k$ -vector space.