Summary of statistical inference.

1) Hypothesis testing. Ho: µ= µo against Ha: µ≠ µo, we compute the z-score $z = \frac{\overline{x} - \mu_0}{5\sqrt{n}}$ If 1212 (1.96) then we reject (95%)
2.33 Ho and accept 98%
2.576) Ha at the 99% level, respectively. Otherwise, we do not. 2) Confidence intervals.

A 95%/98%/99% confidence interval for a population mean is given by the interval $(\overline{\times} - L \cdot \overline{/n}, \overline{\times} + L \cdot \overline{/n}),$ where L= 1.96/2.33/2.576 respectively. We use the same interval for a population proportion p, except in this case $\overline{X} = \hat{\rho}$ (the sample proportion) and $s = \sqrt{\hat{p}(1-\hat{p})}$.

3) In general,
"reject Ho: µ=µo at the p % level"

15 the same as

"µo lies outside the p % confidence

interval for µ."

New topic: the binomal distribution.

A binomial experiment is one with only two possible outcomes, often called a "success" and a failure." Examples:

- (a) flip a coin: we might call "heads" lor "tails") a "success."
- (b) Shoot a free throw: a made shot is a success.
- (c) Crossbreed pea plants: assuming only green or yellow plants can result, we might call "green" a success.

In general, let's write p for P(success).

E.q. for a fair coin, p=1/2; for a free throw, p=shooter's free throw success rate.

NOW, suppose a binomial experiment is repeated a times. Two questions:

(1) what is the expected number of successes?

(2) Green an integer k with 0 = k = n, what is the probability of exactly k successes out of the n trials?

ANSWERS:

(1) On a given trial, since P(success)=p, we would expect p successes.

So, if X; denotes the number of soccesses on the jth trial, then $E(X_j)=p$.

If X denotes the total number of successes at of n treals, then

$$E(X) = E(X_1 + X_2 + \dots + X_n)$$

$$= E(X_1) + E(X_2) + \dots + E(X_n)$$

$$= p + p + \dots + p = np.$$

Example:

An 80% free throw shooter takes 15 shots in a game. The expected number of made shots is

(2) We can think of it this way:

(a) There are (k) of distributing the k

successes awang the n trials.

(b) For each of these ways, each of the k
successes has probability p, and each of
the n-k failures has probability 1-p. So
the probability of the k successes and n-k
failures happening together is $k(1-p)^{n-k}$

(J) SO:

Plexactly k successes in n trials = (k)pk (1-p).

Example! if an 80% free throw shooter takes 15 shots,

 $P(\text{exactly 12 made shots}) = (15) \cdot (0.8)^{12} \cdot (0.2)^{3}$

≈ 0.250 = 25%.

Thought experiment: without doing any competation, put these numbers (in the above free-throw context) in increasing order:

P(11 made), P(12 made), P(13 made).