Wednesday, 2/28 - 1
The Principle of Mathematical Induction.
(a proof template for statements of the
Yne/N: A(n).)
I dea: let A(n) be a statement about a natural number n.
Example:
Example: $1+2+3++n=\frac{h(n+1)}{2}$
Suppose we can show that:
(1) A(1) is true, and
(a) Whenever $A(k)$ is true for $k \in N$, $A(k+1)$ follows. In other words,

(a) Whenever A(k) is t A(k+1) follows. In YKEIN, A(K) => A(K+1).

Then by (1), A(1) holds, so by (2), A(2) holds, so by (2), A(4) holds... so "ultimately," A(n) holds for any nEN.

So we have a "mathematical induction" proof template:

Theorem. YneW, A(n). Step 1: Is A(1) true? [Prove A(11.]
So A(1) is true.

Step 2: Assume A(k). [Now do what's

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necesary to conclude: ] Therefore, A(k+1).
So A(k) = A(k+1).
   So by the principle of mathematical induction, A(n) is tree Yn E/No
     shorks

Step 1 is the "base step."

Assuming A(k) is the "induction hypothesis."

Deducing A(k+1) is the "inductive step."
Example:
Prove that, \forall n \in IN, 1+2+3+...+n = \frac{n(n+1)}{2}
            A(n) be the statement
 Step 1: 15 A(1) true?
    So A(1) is true.
 Step 2: Assume
               A(k): 1+2+3+...+ k= k(k+1).
    To deduce A(k+1), we note that
 1+2+3+... + k+1 = (1+2+3+...+ k)+ k+1
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