Definition 1. A set is a collection of objects, called elements Ways of describing Idefining ldenoting sets: · symbols/hames · listing elements " set builder notation. Examples. symbol/hane "mathematik verquoque" = Ea,e, a, h, b, k,m, n, r, t, u, v & listings (order = { m, a, th, e, i, k, v, r, q, n, v} doesn't watter.
= { letters & a is a letter in } mathematikvergnugens braces 23 mean "the set of all " and the colon": means "such that a) Z = the set of all integers = \(\frac{1}{2}, \ = { 0, ± 1, ± 2, ...

The symbol I is reserved for the set of

3) $E = the set of even integers = <math>\frac{1}{2}$ 0, t^2 1, t^4 1, ... $\frac{1}{2}$ 1 belongs to "or "is an element of"

6) In general, for a, b \(\mathbb{Z}, \) a + b \(\mathbb{Z} \) denotes \(\lambda \) \(\mathbb{Z} \) \(\mathbb{N} = \alpha + b k \) for some
$$k \in \mathbb{Z}_3^2$$
.

Fig. the set E above may be denoted $O + \lambda \mathbb{Z}_4$, also written $\lambda \mathbb{Z}_6$.

8)
$$SL(2,\mathbb{Z}) = \{ \text{matrices } (ab) : a,b,c,d \in \mathbb{Z}, ad-bc = 1 \}$$

9) More special, reserved symbols:

Definition 2.

Let A, B be sets. We say A is a subset of B, written $A \leq B$, if every element of A is also in B (that is: if no element of A lies outside of B).

E.g. for the sets defined above:

N = 1 ; Z = R (we can write N = Z ⊆ R); 2+7Z ⊆ Z; [-3,5) ⊆ R; F ⊆ E;

 $\{\{1,2\}\}\subseteq\{\{1,2\},\{3\}\},\$ $\emptyset\subseteq any set whatsoever;$ any set whatsoever \subseteq itself.

Definition 3

The cardinality of a set 5, denoted 151, is the number of elements of 5.

E.g. for the sets above,

|F|=6, |L|=12, |\$/=0,

|IN| = |O| = |IR| = |E-3,5| = |E| = |2+7Z| = |5L(2,Z)|= ∞ .