Two strains of bacteria —  $Calcul\ S.\ Coli$ , denoted C, and  $Life\ S.\ Eyencus$ , denoted L — are dissolved in a solution of Sprite, denoted S. Below, is a verbal description of the interactions among the two types of bacteria and the Sprite.

- ullet C grows logistically, with carrying capacity proportional to the amount of L present.
- Sprite consumes C at a rate proportional to the amount of C present.
- A pair of C bacteria can spontaneously join to form an L bacterium; the overall rate at which this occurs is proportional to the number of possible C-to-C interactions;
- L grows at a rate that is, in the absence of other factors, proportional to the amount of L present, but that is inhibited by S: the more S there is present, the more slowly L grows;
- An L bacterium can spontaneously split into two C bacteria; the overall rate at which this occurs is proportional to the amount of L present;
- S grows at a rate proportional to the amount of C present times the amount of L present;
- Each *individual* C bacterium consumes S at a rate proportional to the amount of S present;
- L consumes Sprite at a rate proportional to the amount of L present.

$$+tL$$
  $-eS$   $+d(L+eS)$   $+aC\left(1-\frac{CL}{b}\right)$ 

$$C' = +aC\left(1 - \frac{C}{bL}\right) - wC - 2\ell C^2 + 2tL$$

$$L' = +\ell C^2 + \frac{dL}{1 + eS} - tL$$

$$S' = +gCL - vCS - hL$$