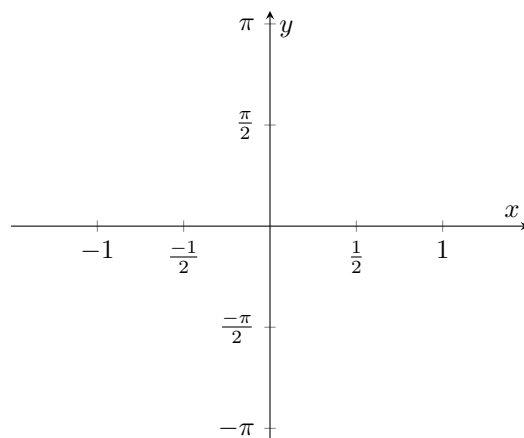
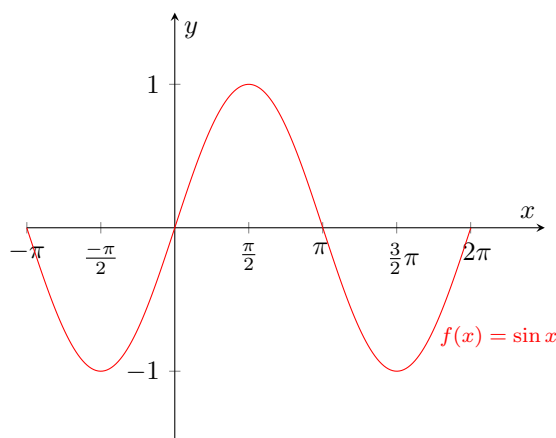


## Lecture: Section 3.6: Inverse Trig Functions

*Lecturer: Sarah Arpin***Today's Goal: We start this on Wednesday, finish on Friday.**

Logistics: Friday there is a check-in!

**Warm-Up 1.1** True or False:  $\frac{d}{dx} \ln(10) = \frac{1}{10}$ **1.1**  $\text{Arcsin}(x)$ 

Recall how to do computations with inverse trig functions:

$$\cos(\arcsin(\frac{-1}{2})) =$$

To find the derivative of  $\arcsin(x)$ , we will use a property of inverse function along with implicit differentiation, and some properties of trig functions. The necessary property:

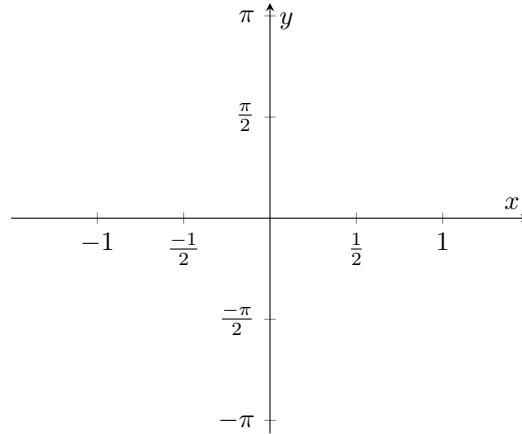
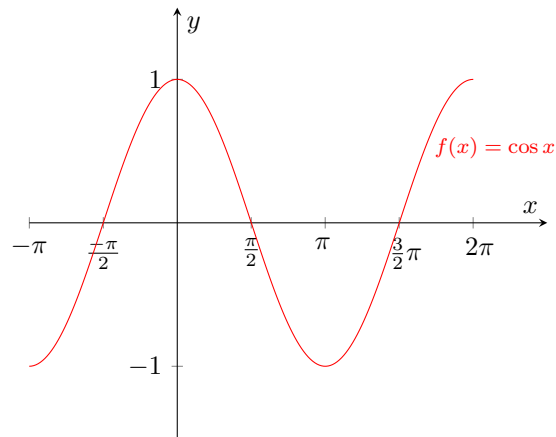
$$\sin(\arcsin(x)) = x$$

Note that this only holds for  $x$  in the interval:

In summary:

$$\frac{d}{dx} \arcsin(x) = \frac{1}{\sqrt{1-x^2}}$$

## 1.2 $\text{Arccos}(x)$



Again with the domain restriction in mind, we can use a similar process to find the derivative of  $\arccos(x)$ :

$$\cos(\arccos(x)) = x$$

### 1.3 $\text{Arctan}(x)$

$$\frac{d}{dx} \arctan(x) = \frac{1}{1+x^2}, \text{ on the domain of } \arctan(x) \text{ which is } -\pi/2 < x < \pi/2$$

### 1.4 Examples

Evaluate:

**Example 1.2**  $\csc(\arccos(3/5)) =$

**Example 1.3**  $\cos(\arcsin(1/2)) =$

Find the derivatives of the following functions:

**Example 1.4**  $y = \arctan\left(\frac{x^2-1}{x^2+2}\right)$

**Example 1.5**  $f(x) = e^{\arcsin(x^2)+3x+1}$