$\qquad$

To receive full credit you must show work.

1. Improper Integrals:
(a) [2 points] Infinity is weird!! In your own words (1-3 sentences), explain why we need limits to make sense of improper integrals.
(b) [2 points] Rewrite $\int_{1}^{\infty} \frac{1}{x^{2}} d x$ and $\int_{-2}^{3} \ln |t| d t$ using limits as necessary (If you have time, do they converge or diverge?).
2. Partial Fractions:
(a) [3 points] Decompose the following into partial fractions (you do not need to solve for the coefficients):

$$
\frac{x^{4}-x^{3}+2 x+1}{(x-3)^{3}\left(x^{2}+9\right)}=
$$

(b) $[\mathbf{3}$ points $]$ Find $\int \frac{2 x+1}{(x-2)(x+3)} d x$

