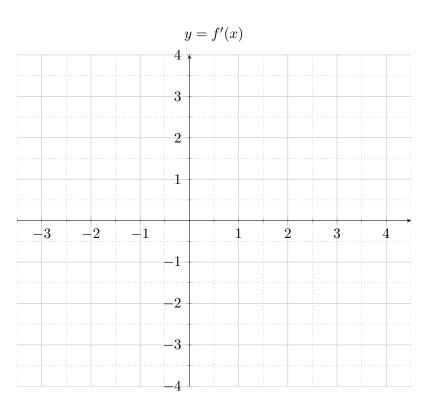
1. The purpose of this problem is to see how to construct a derivative function one point at a time by looking at a graph.

Background review: estimating derivatives, one point at a time:

- The derivative of a function at a point represents the slope (or rate of change) of a function at that point.
- If you have a graph, you can estimate the derivative one point at a time by drawing the tangent line at that point, then calculating the slope of that tangent line (remember, slope is rise over run).
- (a) Go to the website http://www.shodor.org/interactivate/activities/Derivate/
- (b) Enter the function  $y = x^2 x 2$ . Use the tool to calculate the slope of the graph at each of the points x = -1, 0, 1, 2 and 2.5. Enter the values of the slope in the following table:

(c) Now plot these points and connect them smoothly to see a graph of f'(x)



(d) What do you think the formula for this graph is?

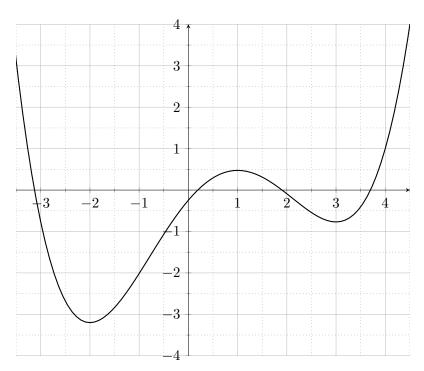
- 2. In this problem, you'll calculate the derivative of the same function as the previous problem, but this time you'll do it analytically (with formulas)
  - (a) Calculate the derivative of  $f(x) = x^2 x 2$ .  $f'(x) = \lim_{h \to 0} \frac{f(x+h) f(x)}{h} =$

- (b) Do your results from this problem match your results from the last problem?
- 3. Khan academy has an exercise that gives a good visual and tactile experience of producing the derivative function point by point. Do at least one exercise on this website:

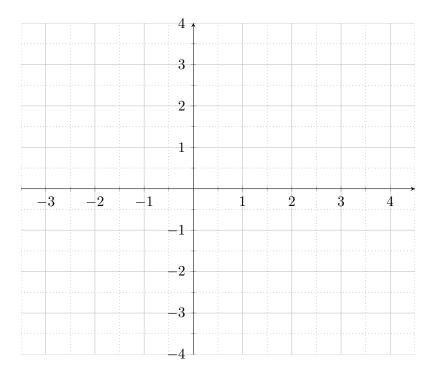
http://www.tinyurl.com/math1300-week4

In the space below, sketch the graph of f(x) and f'(x) from one of the exercises you did.

4. Below is a graph of a function.



Without the aid of technology, use the graph of the function above to sketch a graph of its derivative function on the axes below.



- 5. Based on your experience above, what seems to be true about the relationship between f(x) and f'(x)?
  - (a) Where f(x) is increasing, f'(x) is
  - (b) Where f(x) is decreasing, f'(x) is
- 6. Below are some more involved questions. We will be addressing these in the coming sections. Do you have any guesses for these?
  - (a) Where f(x) is concave up, f'(x) is \_\_\_\_\_\_.
  - (b) Where f(x) is concave down, f'(x) is \_\_\_\_\_\_.
  - (c) Where f(x) is \_\_\_\_\_\_, or \_\_\_\_\_\_, f'(x) is undefined.
  - (d) What will the derivative be when f(x) has a relative high point (maximum) or relative low point (minimum)?
  - (e) If the derivative is 0 at a point, what are all the ways the original function could look?
  - (f) What about if the derivative has a relative maximum or minimum?