

Math 6010 - Assignment 5

Due October 9, 2023

- (1) Show that the following are primitive recursive predicates:
- (a) x divides y ;
 - (b) x is prime.

- (2) Let P be a k -ary primitive recursive predicate. Show that

$$f(\bar{x}, y) := \mu(t < y) P(\bar{x}, t)$$

is primitive recursive.

- (3) Show that the Diagonal Halting Problem

$$K := \{x \in \mathbb{N} \mid \varphi_x(x) \text{ is defined} \}$$

is computably enumerable but not computable.

- (4,5) Show that Σ_n^0 for $n \in \mathbb{N}$ is closed under \wedge, \vee and bounded quantifiers.