Math 2135 - Practice Final

December, 2024

- (4) Let A be the standard matrix for the rotation r of \mathbb{R}^2 by angle φ counterclockwise around the origin. What are the eigenvalues and eigenvectors of A? Can A be diagonalized over the reals?
- (5) Diagonalize A if possible. Also compute det A. Is A invertible?

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 0 & 3 \\ 0 & 0 & -2 \end{bmatrix}$$

(6) Compute the inverse if possible:

$$A = \begin{bmatrix} 1 & -2 \\ -2 & 4 \end{bmatrix}, \quad B = \begin{bmatrix} 1 & 2 & 4 \\ 0 & 0 & -1 \\ 1 & -1 & 0 \end{bmatrix}$$

(7) Let $h: V \to W$ be a linear map, let $v_1, \ldots, v_k \in V$ such that $h(v_1), \ldots, h(v_k)$ are linearly independent. Show that v_1, \ldots, v_k are linearly independent.