Discrete Probability Theory

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If we assume that all hands are equally likely and that hands are chosen at random, then the probability of receiving Two Pair is 2.25 times more likely than the probability of receiving Three of a Kind.

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Classical Discrete Probability Theory

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The probability of an event E is the number of successes
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Picture

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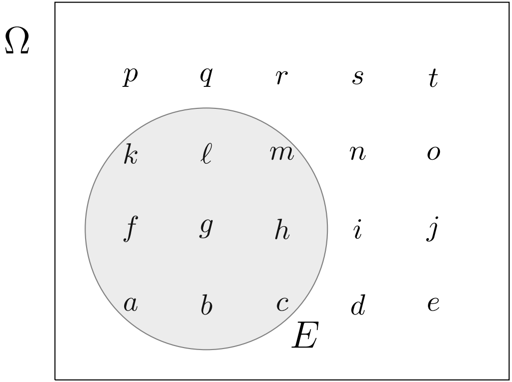

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3. What is the probability that if you flip a fair coin six times you will get 3 or more consecutive heads?