Logic

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5. Once we know how to assign Truth to Statements, we need to analyze how Truth is preserved in Deductions.

Examples: $\langle$Things; Language elements$\rangle$

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Example 1.

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Example 1. (The natural numbers)

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Exercise! What symbols do we need to add to our language to be able to write or speak about these Things?