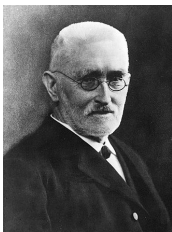
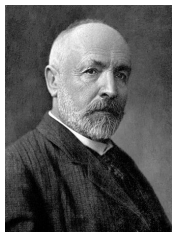


The Cantor-(Dedekind)-Bernstein-Schröder Theorem



The Cantor-Bernstein-Schröder Theorem

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- 2 (1887) Dedekind discovers a proof but does not publish it.
- 3 (1897) Bernstein gave a proof in Cantor's seminar.
- 4 (1897) Schröder announces a proof.
- 5 (1897) Dedekind discovers a second proof.
- 6 (1898) Bernstein's proof is published in his PhD thesis.
- 7 (1898) Schröder publishes his proof, which turned out to be wrong.