

Logic Topics.

- (1) Structures.
 - (a) The real numbers
 - (b) Real vector spaces
 - (c) Metric spaces
 - (d) A universe of sets
- (2) Alphabet of symbols.
 - (a) variables: $x_0, x_1, x_2, x_3, \dots$
 - (b) logical symbols
 - (i) logical connectives: $\wedge, \vee, \neg, \rightarrow, \leftrightarrow$.
 - (ii) quantifiers: $\exists, \forall$
 - (c) nonlogical symbols: operation symbols, predicate symbols (including $=$).
 - (d) punctuation: parentheses, commas.
- (3) Formulas and sentences.
 - (a) terms
 - (i) Polish notation
 - (ii) unique readability
 - (iii) parse trees
 - (b) atomic formulas
 - (c) formulas
 - (d) quantifiers, scope of a quantifier, free and bound variables
 - (e) sentences, complexity of quantification
- (4) Meaning
 - (a) Interpreting the nonlogical symbols
 - (b) The effect of logical connectives on predicates
 - (c) Logical equivalence. Prenex form.
- (5) Semantic entailment.
- (6) Proof.
- (7) The Completeness Theorem.