

Category Theory

Homework Assignment VI

For everyone: Read 4.3 of Riehl and 4.3 of Mac Lane.

For Oscar, Khizar, Paige, Nate: Present the problems below on October 25.

PROBLEMS

1. Describe the unit and counit of the adjunction (Δ, Π, φ) that defines products in $\mathcal{C} = \mathbf{Set}$:

$$\Delta: \mathcal{C} \rightarrow \mathcal{C} \times \mathcal{C}: A \mapsto (A, A); \quad \Pi: \mathcal{C} \times \mathcal{C} \rightarrow \mathcal{C}: (X, Y) \mapsto X \Pi Y.$$

2. Let \mathcal{C} be a category with small coproducts. Show that a functor $U: \mathcal{C} \rightarrow \mathbf{Set}$ has a left adjoint if and only if U is representable.

3. Exercise 1.7.ii of Riehl.

4. Exercise 4.3.iii of Riehl.