

ALGEBRA 1

HOMEWORK ASSIGNMENT VIII

(Turn in underlined problems.)

Read Sections 8.1-8.3, 9.1-9.4.

<u>SECTION</u>	<u>PROBLEMS</u>
7.1	5, 7, 10, 14, 28
7.2	4, 7, 12, 13
7.3	2, 5, 10, 13, 26
7.4	8, 13, 30
7.6	<u>1</u> , 3
8.1	8, <u>10</u>
8.2	5, <u>6</u> , 7
8.3	4, 11

ADDITIONAL PROBLEMS

Challenge Problem! (Prize = 1 foreign coin.)

Jacobson's Theorem asserts that any ring that satisfies an identity of the form $x^n = x$, for some fixed $n > 1$, is commutative. The proof uses the axiom of choice. Prove a special case of Jacobson's Theorem by showing that any ring satisfying $x^4 = x$ is commutative, but do not use the axiom of choice. Just deduce $xy = yx$ directly from $x^4 = x$ and the identities defining rings.