University of Colorado Department of Mathematics Problem of the Month October 2010

Let u_1, \ldots, u_n be vectors in \mathbb{R}^d such that $u_1 + \cdots + u_n = 0$ and $|u_i| \ge 1, i = 1, \ldots, n$. Prove that, for every vector v,

 $|u_1 - v| + \dots + |u_n - v| \ge n$