University of Colorado Department of Mathematics

Problem of the Month October 2009

Prove that

$$(\cos x)^{(\cos^2 x)} > (\sin x)^{(\sin^2 x)}$$
 and $(\cos x)^{(\cos^4 x)} < (\sin x)^{(\sin^4 x)}$ when $0 < x < \pi/4$.