University of Colorado Department of Mathematics Problem of the Month November 2012

Show that, if f_1, f_2, \ldots, f_n are nonnegative continuous functions defined on the interval [0, 1], and $\int_0^1 f_k = a_k$ for all k, then there exists some $x \in [0, 1]$ such that $f_1(x)f_2(x)\cdots f_n(x) \leq a_1a_2\cdots a_n$.