University of Colorado Department of Mathematics Problem of the Month November 2008

Find all polynomials of the form

 $x^n \pm x^{n-1} \pm x^{n-2} \pm \dots \pm x \pm 1$

that have only real roots (all coefficients are ± 1 , no term is missing).