University of Colorado Department of Mathematics Problem of the Month March 2014

Let $Q = \{2, 3, 4, 5, 7, 8, 9, 11, \dots\}$ be the set of prime powers. Find all polynomials f(x) with integer coefficients such that $f(Q) \subseteq Q$.