University of Colorado Department of Mathematics Problem of the Month March 2013

Find all continuously differentiable functions $f \colon \mathbb{R} \to \mathbb{R}$ having the property that for every integer n and every odd integer a there is an odd integer b such that $f\left(\frac{a}{2^n}\right) = \frac{b}{2^n}$.