University of Colorado Department of Mathematics

Problem of the Month February 2010

Given a > 0, define $S_n = a^n + \frac{1}{a^n}$ for n > 0. Prove that if S_k and S_{k+1} are both integers for some k, then S_n is an integer for all n.