University of Colorado Department of Mathematics Problem of the Month December 2011-January 2012

Assume that a convex polyhedron is contained inside a sphere of radius R. Denote its edges by E_1, \ldots, E_n . Let L_i be the length of E_i and assume that the faces meet at E_i at the angle γ_i . Show that

$$\sum_{i=1}^{n} L_i(\pi - \gamma_i) \le 8\pi R.$$