University of Colorado Department of Mathematics

Problem of the Month April 2009

Show that for every real number x and for every natural number n it is the case that

$$\frac{x}{1+x^2} + \frac{x}{2^2+x^2} + \dots + \frac{x}{n^2+x^2} < \frac{\pi}{2}.$$