University of Colorado Department of Mathematics Problem of the Month April 2011

Define a sequence of real numbers by $a_0 = 0, a_1 = 1, a_2 = 1$ and $a_{k+3} = 2a_{k+2} + 2a_{k+1} - a_k$

for all $k \ge 0$. Show that a_n is the square of an integer for all $n \ge 0$.