

1. (2 points) Consider a function f that has values given in the following table:

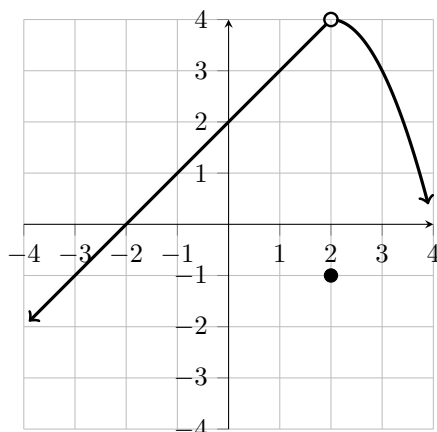
x	1.5	1.9	1.99	1.999	1.9999
$f(x)$	2.2500	3.6100	3.9601	3.9960	3.9996

From the above information, what can you conclude about $f(x)$ at $x = 2$?

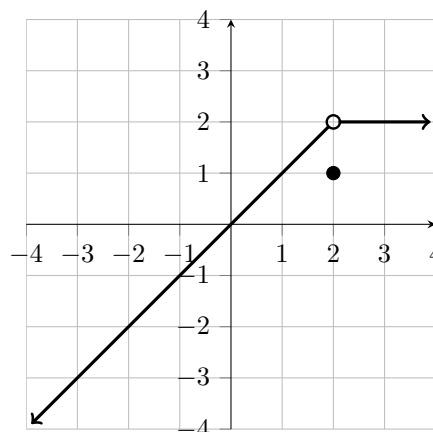
- (a) $f(x)$ is undefined at $x = 2$.
(b) $f(x)$ approaches 4 as x approaches 2 from the left.
 (c) $f(x)$ approaches 4 as x approaches 2 from the right.
 (d) $f(2) = 4$.
 (e) $f(x)$ approaches 4 as x approaches 2 from both sides.

The values in the table are all to the left of $x = 2$.

2. (2 points) Use the graphs of $f(x)$ and $g(x)$ to calculate the limit.



$f(x)$



$g(x)$

$$\lim_{x \rightarrow 2} (f(x) \cdot g(x)) =$$

(a) 8

(b) 4

(c) -1

(d) -8

(e) The limit does not exist

① Note: $\lim_{x \rightarrow 2} f(x) = 4$ and $\lim_{x \rightarrow 2} g(x) = 2$

② Since both exist,

$$\begin{aligned} \lim_{x \rightarrow 2} (f(x) \cdot g(x)) &= \lim_{x \rightarrow 2} f(x) \cdot \lim_{x \rightarrow 2} g(x) \\ &= 4 \cdot 2 \\ &= 8 \end{aligned}$$

3. (2 points) Compute $\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2}$ if it exists.

(a) 0

(b) 1

(c) 4

(d) 6

(e) The limit does not exist

Factor & Cancel:

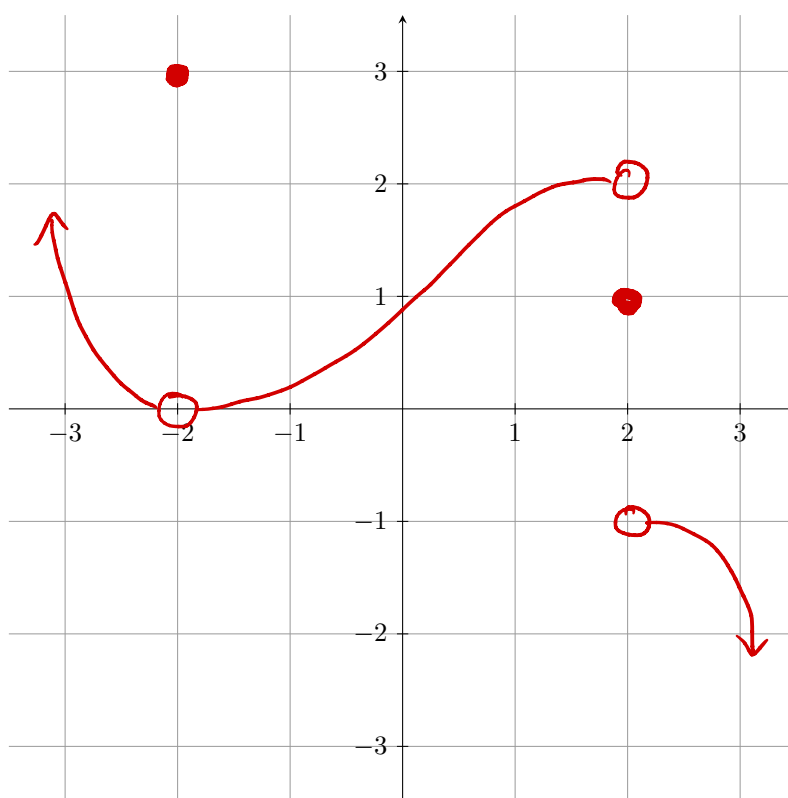
$$\lim_{x \rightarrow 2} \frac{x^2 - 4}{x - 2} = \lim_{x \rightarrow 2} \frac{(x+2)(\cancel{x-2})}{(\cancel{x-2})}$$

$$= \lim_{x \rightarrow 2} x + 2 = \lim_{x \rightarrow 2} x + \lim_{x \rightarrow 2} 2$$

$$= 2 + 2$$

$$= 4$$

4. (4 points) Draw the graph of a function f , whose domain contains $[-3, 3]$, that satisfies the properties below. Sketch your graph on the grid.



- $f(2) = 1$ ✓
- $f(-2) = 3$ ✓
- $\lim_{x \rightarrow 2^+} f(x) = -1$ ✓
- $\lim_{x \rightarrow 2^-} f(x) = 2$ ✓
- $\lim_{x \rightarrow -2} f(x) = 0$ ✓

There are many possible answers!