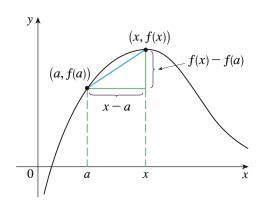
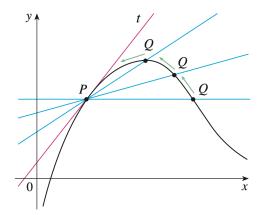
## 2.7 Derivatives and Rates of Change

Question. What is the story so far?

## Definition.

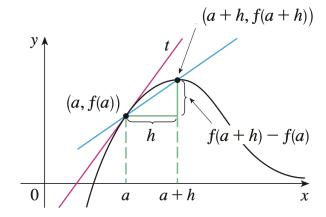
- What is the slope of the secant line through (a, f(a)) and (x, f(x))?
- What is the slope of the tangent line at (a, f(a))?





**Example.** Find an equation of the tangent line to the parabola  $y = x^2$  at the point (1,1).

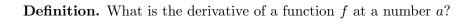
**Definition.** What is another way to write the slope of the tangent line through (a, f(a))?



**Example.** Find an equation of the tangent line to the hyperbola  $y = \frac{3}{x}$  at the point (3,1).

**Example.** Suppose that a ball is dropped from 450 m above the ground.

- What is the velocity of the ball after 5 seconds?
- How fast is the ball traveling when it hits the ground?





**Example.** Find an equation of the tangent line to the parabola  $f(x) = x^2 - 8x + 9$  at the point (3, -6).