Introduction

Linear functions are some of the simplest and most widely used functions in mathematics. They are used to model real-world relationships, such as distance over time or cost over quantity. This lecture covers the fundamentals of linear functions, how to find their equations, and how to apply them to solve problems.

Overview of Line Forms

Form	Equation	Notes
Slope-Intercept		m is the slope, b is the y -intercept
Point-Slope		m is the slope, (x_1, y_1) is a point on the line
General		a,b,c are constants
Horizontal Line		m = 0, constant y-value
Vertical Line		Undefined slope, constant x -value

Slope-Intercept Form

Example. Write the equation of a line with a slope of 3 and a y-intercept of -2.

Point-Slope	Form
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Example. Find the equation of the line passing through the points (1,2) and (3,6).

Parallel and Perpendicular Lines

Definition.

- Two lines are parallel if ______ .
- ullet Two lines are perpendicular if ______ .

Example: Determine if the lines y = 2x + 3 and $y = -\frac{1}{2}x - 4$ are perpendicular.

Modeling Situations with Linear Function	Modeling	Situations	with Line	ar Function
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Example: A company charges a flat fee of \$5 for delivery and \$2 per mile. Write a linear function that models the total cost C based on the number of miles x.

General Form of a Line

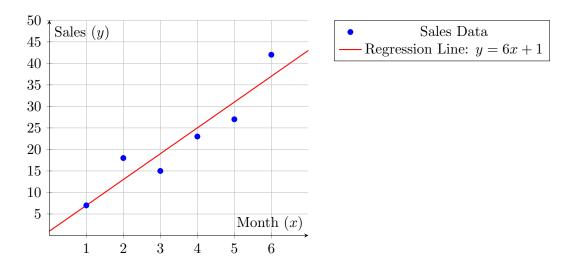
Example. Convert y = 2x + 3 to general form.

Application: Data Analysis & Trend Lines

Linear models are essential in data analysis for understanding trends and making predictions. Imagine a company tracks its sales over six months. The data points are:

Month (x)	Sales (y) in \$1000s	
1	7	
2	18	
3	15	
4	23	
5	27	
6	42	

The scatter plot below shows this data, and the regression line models the trend.



The regression line is y = 6x + 1. Using the regression line, we can predict future sales. For example, what does the model predict for the sales in Month 8?