# Exercise 2.6.9 <br> Introduction to Discrete Mathematics <br> MATH 2001 

SEBASTIAN CASALAINA

Abstract. This is Exercise 2.6.9 from Hammack [Ham13, §2.6]:

Exercise 2.6.9. Decide whether the pairs of statements $p \wedge q$ and $\sim(\sim P \vee \sim Q)$ are logically equivalent.

Solution. The two statements are logically equivalent. Indeed, considering the truth table

| $p$ | $q$ | $p \wedge q$ | $\sim p \vee \sim Q$ | $\sim(\sim P \vee \sim Q)$ |
| :---: | :---: | :---: | :---: | :---: |
| $T$ | $T$ | $T$ | $F$ | $T$ |
| $T$ | $F$ | $F$ | $T$ | $F$ |
| $F$ | $T$ | $F$ | $T$ | $F$ |
| $F$ | $F$ | $F$ | $T$ | $F$ |

we see that the columns for $p \wedge q$ and $\sim(\sim P \vee \sim Q)$ are the same, so that the two statements are logically equivalent.

## References

[Ham13] Richard Hammack, Book of proof, Creative Commons, 2013.

University of Colorado, Department of Mathematics, Campus Box 395, Boulder, CO 80309
Email address: casa@math.colorado.edu

