## Math 2001: PHW4

## Due: February 10, 2016

- 1. From the book do:
  - 2.10: 2, 6, 10
  - 5: 2, 4
  - 6: 4, 6, 14
- 2. Identify whether each of the following statements is true or false. If it is true, prove it. If it is false, then provide a counterexample.
  - (a) Let A, B, and C be sets. Then

$$(A \cap B) \cup C = A \cap (B \cup C).$$

- (b) If  $a, b \in \mathbb{Z}_{\geq 1}$  and both  $\sqrt{a}$  and  $\sqrt{b}$  are irrational, then  $\sqrt{ab}$  is irrational.
- 3. A point (m,n) in  $\mathbb{R}^2$  is a *lattice point* if both  $m,n\in\mathbb{Z}$ . Prove that the number of lattice points inside any circle centered at the origin is a number of the form 4k+1 for some integer k (note that you don't have to say what k is).

Hint: Split the set of lattice points into subsets, depending on the quadrants.