# 02.05 Limits Involving Infinity

Tuesday, September 8, 2020

9:36 AM



Math 1300: Calculus I

Fall 2020

Lecture 6: Section 2.5: Limits Involving Infinity

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Today's Goal: To describe limits that go to infinity, and limits as x goes to infinity.

Logistics: Check-in 4 will cover continuity, discontinuities, and limits involving infinity.

Check-in 5 will cover limits involving infinity

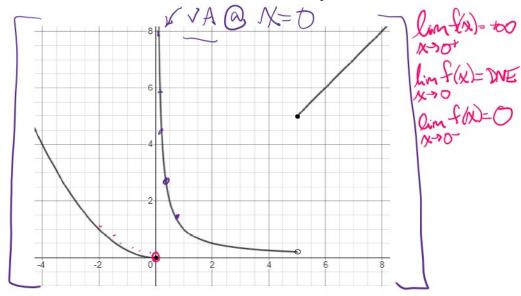
Check out the parent functions pdf in "Weekly work" on Canvas

Please enail me when you send me a question on verassign

Warm-Up 6.1 True or False:  $f(x) = \frac{x-1}{\sqrt{x^2+3}}$  is continuous on  $(-\infty, \infty)$ .

Infinite Limits: Vertical Asymptotes 6.1

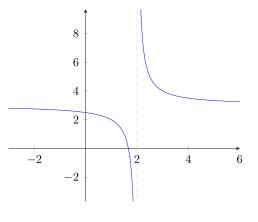
We have had some informal discussion about this before. Recall this example from our Section 2.2 Notes:



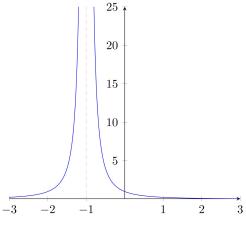
We discussed  $\lim_{x\to 0^+} f(x)$  and concluded that this limit does not exist (because it's not approaching a real number as we get closer to 0 from the right), but we can do better than that: We can specify that the function values are approaching positive infinity. We do this by writing:

$$\lim_{x \to 0^+} f(x) = \infty.$$

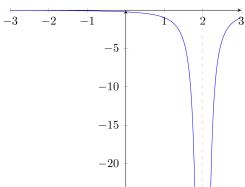
This is an infinite limit. We use  $\pm \infty$  and "DNE" to distinguish between different types of vertical asymptotes:



linf(x)= DNE



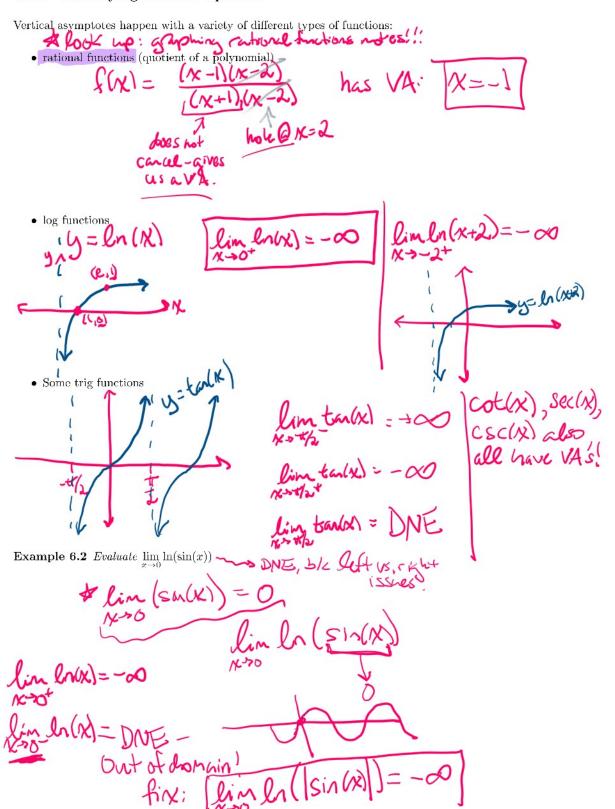
linf(x)=+00



-25

limf(X)=-01

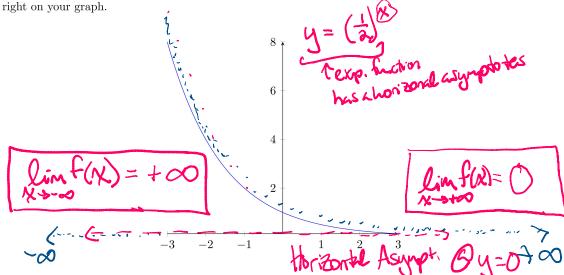
## 6.1.1 Identifying from an equation



## 6-4

#### 6.2Limits as x approaches $\pm$ Infinity

We can also consider limits as x itself goes to  $\pm \infty$ : Think of walking very far to the left or very far to the



If you don't have the graph to look at, you can plug in very large values of x to see the limit as  $x \to \infty$  (like

1000, etc.), or very negative numbers to see the limit as  $x\to -\infty$  (like -1000). -- as long as you know what to expect from that typesh furtion

**Definition 6.3** The line y = L (where L is some constant number) of the curve y = f(x) if either

$$\lim_{x \to \infty} f(x) = L \text{ or } \lim_{x \to -\infty} f(x) = L$$

### 6.3 Pre-calc Techniques

You have experience finding horizontal asymptotes of rational functions! Consider a rational function of the form

$$\frac{f(x)}{g(x)}$$

where f and g are polynomials. How do you find the horizontal asymptote of such a function?

- If the degree of f(x) is smaller than the degree of g(x),
- If the degrees of f(x) and g(x) are the same,
- If the degree of f(x) is larger than the degree of g(x),

**Example 6.4** Find the equation for the horizontal asymptote of the function  $f(x) = \frac{3x^2 - 2x}{x - 2x^2}$ 

Example 6.5 Evaluate the following limits:

1. 
$$\lim_{x \to -\infty} \frac{x^2 - 3}{x^5 + 1}$$

$$2. \lim_{x \to \infty} \left(\frac{1}{2}\right)^x$$

3. 
$$\lim_{x \to -\infty} \frac{2}{x^3}$$

4. 
$$\lim_{x \to \infty} e^x$$