

## Derivatives of common functions

You have to know all of this forever and ever.

- Constants don't change:

$$\frac{d}{dx}(c) = 0, \quad c \in \mathbb{R}.$$

- Linearity:

$$\frac{d}{dx}(f(x) + g(x)) = \frac{df}{dx} + \frac{dg}{dx}, \quad \frac{d}{dx}(cf(x)) = c \frac{df}{dx}, \quad c \in \mathbb{R}.$$

- Product rule:

$$(fg)' = f'g + fg'$$

- Quotient rule:

$$\left(\frac{f}{g}\right)' = \frac{gf' - fg'}{g^2}$$

- Chain rule:

$$[f(g(x))]' = f'(g(x))g'(x)$$

- Fundamental theorem of calculus: Suppose  $f$  is continuous on an open interval containing  $a$  and  $x$ .

$$\text{If } F(x) := \int_a^x f(t)dt, \text{ then } \frac{dF}{dx} = f.$$

- Power functions:

$$\frac{d}{dx}(x^n) = nx^{n-1}.$$

- Exponential and logarithmic functions:

$$\frac{d}{dx}(a^x) = a^x \ln a, \quad \frac{d}{dx}(\log_a x) = \frac{1}{x \ln a}, \quad \text{for } a > 0 \text{ constant}$$

- Trigonometric functions:

$$\begin{aligned} (\sin x)' &= \cos x, & (\cos x)' &= -\sin x, & (\tan x)' &= \sec^2 x, \\ (\csc x)' &= -\csc x \cot x, & (\sec x)' &= \sec x \tan x, & (\cot x)' &= -\csc^2 x. \end{aligned}$$

- Inverse trigonometric functions:

$$\frac{d}{dx}(\arcsin x) = \frac{1}{\sqrt{1-x^2}}, \quad \frac{d}{dx}(\arccos x) = \frac{-1}{\sqrt{1-x^2}}, \quad \frac{d}{dx}(\arctan x) = \frac{1}{1+x^2},$$