

Collaborators (if any):

Due Monday, March 12th at the beginning of class. Submit your work on additional paper, treating this page as a cover sheet. You may use technology and work with with other students. If you work with others, please list their names above.

Choose five of the series below and CAREFULLY write a detailed argument for its convergence or divergence.

1.
$$\sum_{n=1}^{\infty} \frac{n}{n^3 + 1}$$

2.
$$\sum_{n=1}^{\infty} \frac{n^2 + 1}{n^3 + 1}$$

3.
$$\sum_{n=1}^{\infty} \frac{n^3}{5^n}$$

4.
$$\sum_{n=1}^{\infty} \frac{(-1)^n}{\sqrt{n+1}}$$

5.
$$\sum_{n=2}^{\infty} \frac{1}{n\sqrt{\ln n}}$$

6.
$$\sum_{n=1}^{\infty} \ln\left(\frac{n}{3n+1}\right)$$

7.
$$\sum_{n=1}^{\infty} (-1)^{n-1} \frac{\sqrt{n}}{n+1}$$

8.
$$\sum_{n=1}^{\infty} \frac{\cos(3n)}{1 + (1.2)^n}$$

9.
$$\sum_{n=1}^{\infty} \frac{1 \cdot 3 \cdot 5 \cdots (2n-1)}{5^n n!}$$

10.
$$\sum_{n=1}^{\infty} \left(\frac{1+n}{3n}\right)^n$$

11.
$$\sum_{n=1}^{\infty} (1 - \cos(1/n))$$

[Hint: compare to $\sum_n \frac{1}{n^2}$.]

12.
$$\sum_{n=1}^{\infty} \frac{8^n}{n!}$$

13.
$$\sum_{n=1}^{\infty} \frac{(-1)^{n-1} 2^n}{n^2}$$

14.
$$\sum_{n=1}^{\infty} \frac{\cos(n\pi)}{n}$$

15.
$$\sum_{n=1}^{\infty} \frac{\tan(1/n)}{n^{3/2}}$$

16.
$$\sum_{n=1}^{\infty} \frac{(-1)^n}{2 + \sin n}$$

17.
$$\sum_{n=1}^{\infty} \sin(1/n^2)$$

18.
$$\sum_{n=1}^{\infty} \cos(1/n^2)$$

19.
$$\sum_{n=1}^{\infty} \tan(1/n^2)$$

20.
$$\sum_{n=1}^{\infty} n e^{-n^2}$$