## Math 2002 Number Systems Homework Set 1

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**Problem 1:** Using truth tables determine which ones of the following propositional formulas is a tautology:

- a)  $(A \Longrightarrow B) \iff (\neg A \lor B)$
- b)  $(A \wedge B) \vee (\neg A \vee \neg B)$
- c)  $(A \lor B) \implies (A \land B)$
- $d) (A \wedge B) \implies (A \vee B)$

(8P)

**Problem 2:** For each of the following statements, formulate a logically equivalent one using only A, B,  $\neg$  and  $\lor$ . You may use as many parentheses as you need. Use a truth table or rules of mathematical logic to verify your claim.

- a)  $A \implies \neg B$
- b)  $\neg A \wedge \neg B$
- c)  $A \iff \neg B$

(6P)

**Problem 3:** For each of the following sentences formulate an English sentence that is its negation:

- a) If you study hard you will do well in school.
- b) I will pay my taxes and avoid going to jail.
- c) Horses eat oates or horses eat hav.

(6P)