

University of Colorado  
Department of Mathematics

2022/23 Semester 1

Math 6310 Real Analysis 1

Assignment 4

**Due uploaded to Canvas Friday October 28, 2022 at 11:59 p.m.**

1. Read the Royden-Fitzpatrick textbook, the rest of Chapter 4, including 4.2, 4.3, 4.4, 4.5, and 4.6.
2. Do problems in Royden-Fitzpatrick pp. 84–85, #22, 25, 27; pp. 89–90 #29, 32, 33, 36; pp. 95 – 96, #44.
3. Let  $f$  be the function defined on  $[0, 2]$  by

$$f(x) = \begin{cases} \frac{1}{\sqrt{2-x}}, & \text{if } x \in [0, 2), \\ 0, & \text{if } x = 2. \end{cases}$$

Prove that  $f$  is Lebesgue integrable over  $[0, 2]$ .