Quiz 2

1. Solve $x^2 - 5 = 0$ by using the zero product property.

$$(x-5^{1/2})(x+5^{1/5}) = 0$$
, so $x = 5^{1/2}$ or $-5^{1/2}$

2. Solve $x^2 + 5x = 3$ by completing the square.

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Since $\frac{5x}{2x} = \frac{5}{2}$, we add the square of this to both sides,

$$x^{2} + 5x + \frac{25}{4} = 3 \cdot \frac{4}{4} + \frac{25}{4} = \frac{37}{4}$$

Then, by the square of a sum formula

$$\left(x+\frac{5}{2}\right)^2 = \frac{37}{4}$$

Take the square root of both sides, and you get

$$x + \frac{5}{2} = \pm \frac{\sqrt{37}}{2}$$

Subtract $\frac{5}{2}$ from both sides and you're done:

$$x = -\frac{5}{2} \pm \frac{\sqrt{37}}{2}$$

3. (a) State the quadratic formula.

If
$$ax^2 + bx + c = 0$$
, then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

(b) Use the quadratic formula to solve $8x^2 - 5x - 1 = 0$.

Here
$$a = 8, b = -5$$
 and $c = -1$, so $x = \frac{5 \pm \sqrt{5^2 - 4 \cdot 8 \cdot (-1)}}{2 \cdot 8} = \frac{5 \pm \sqrt{57}}{16}$

4. Solve $x^{2/3} - x^{1/3} - 15 = 0$ by *u*-substitution.

Let $u = x^{1/3}$. Then the equation becomes

$$u^2 - u - 15 = 0$$

This won't factor nicely, so just use the quadratic formula to get u:

$$u = \frac{1 \pm \sqrt{1^2 - 4 \cdot 1 \cdot (-15)}}{2 \cdot 1} = \frac{1 \pm \sqrt{61}}{2}$$

But $u = x^{1/3}$, so to get x, cube both sides to get

$$x = \left(\frac{1 \pm \sqrt{61}}{2}\right)^3$$

5. Solve $3|5 - 7d| + 7 \ge 4$.

First, subtract 7 from both sides,

$$3|5-7d| \ge -3$$

then divide by 3,

$$|5 - 7d| \ge -1$$

Now that all numbers are on the other side of the inequality, we apply the definition of absolute value, which means we consider two cases:

(a) Case 1: $5-7d \ge -1$. In this case, subtract 5 from both sides,

$$-7d \ge -6$$

 $d \leq \frac{6}{7}$

and divide by -7:

(b) Case 2: $-(5-7d) \ge -1$. In this case, multiply both sides by -1 to get rid of the negative:

$$5-7d \leq 1$$
 Subtract 5:
$$-7d \leq -4$$
 and divide by -7:
$$d \geq \frac{4}{7}$$

Putting all this together gives the solution set as

$$\left\{ d \mid \frac{4}{7} \le d \le \frac{6}{7} \right\} \quad \text{or in interval notation} \quad \left[\frac{4}{7}, \frac{6}{7}\right]$$