

1. Speedometer readings for a motorcycle at 12-second intervals are given in the table.

t (s)	0	12	24	36	48	60
v (ft/s)	30	28	25	22	24	27

- Estimate the distance traveled by the motorcycle during this time period using the velocities at the beginning of the time intervals.
- Give another estimate using the velocities at the end of the time periods.
- Are your estimates in parts (a) and (b) upper and lower estimates? Explain.

Use the following definition for area to answer Problems 2 and 3:

Definition: The **area** A of the region S that lies under the graph of the continuous function f is the limit of the sum of the areas of approximating rectangles:

$$A = \lim_{n \rightarrow \infty} R_n = \lim_{n \rightarrow \infty} [f(x_1)\Delta x + f(x_2)\Delta x + \cdots + f(x_n)\Delta x]$$

2. Use the definition of area given above to find an expression for the area under the graph of f as a limit. Do not evaluate the limit.

$$f(x) = x^2 + \sqrt{1 + 2x}, \quad 4 \leq x \leq 7$$

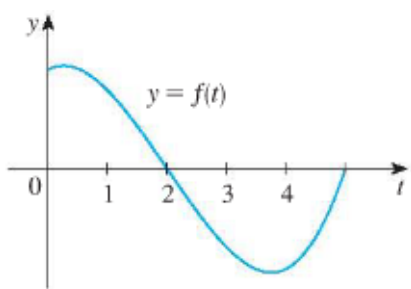
3. (a) Use the definition of area given above to find an expression for the area under the curve $y = x^3$ from 0 to 1 as a limit.
- (b) The following formula for the sum of the cubes of the first n integers is proved in Appendix F of your textbook. Use it to evaluate the limit in part (a).

$$1^3 + 2^3 + 3^3 + \cdots + n^3 = \left[\frac{n(n+1)}{2} \right]^2$$

4. If $\int_1^5 f(x) dx = 12$ and $\int_4^5 f(x) dx = 3.6$, find $\int_1^4 f(x) dx$

5. If $F(x) = \int_2^x f(t) dt$, where f is the function whose graph is given, which of the following values is the largest? Explain your reasoning.

- (a) $F(0)$
- (b) $F(1)$
- (c) $F(2)$
- (d) $F(3)$
- (e) $F(4)$



6. Each of the regions A , B , and C bounded by the graph of f and the x -axis has area 3. Find the value of

$$\int_{-4}^2 [f(x) + 2x + 5] dx$$

