

1. Sketch the graph by hand using asymptotes and intercepts, but not derivatives. Then use your sketch as a guide to producing graphs (with a graphing device) that display the major features of the curve. Use these graphs to estimate the maximum and minimum values.

$$f(x) = \frac{(2x + 3)^2(x - 2)^5}{x^3(x - 5)^2}$$

2. If  $f(x) = \frac{(2x + 3)^2(x - 2)^5}{x^3(x - 5)^2}$ , find  $f'$  and  $f''$  and use their graphs to estimate the intervals of increase and decrease and concavity of  $f$ . Be sure to include graphs of  $f'$  and  $f''$  to fully explain the behavior of  $f$ . Use technology to calculate these derivatives.
3. A rectangular storage container with an open top is to have a volume of  $10 \text{ m}^3$ . Then length of its base is twice the width. Material for the base costs \$10 per square meter. Material for the sides cost \$6 per square meter. Find the cost of materials for the cheapest such container.
4. A cylindrical can without a top is made to contain a volume of 2000 cubic centimeters of liquid. Find the dimensions that will minimize the cost of the metal to make the can.
5. A boat leaves a dock at 2:00 PM and travels due south at a speed of 20 km/h. Another boat has been heading due east at 15 km/h and reaches the same dock at 3:00 PM. At what time were the two boats closest together?
6. The manager of a 100-unit apartment complex knows from experience that all units will be occupied if the rent is \$800 per month. A market survey suggests that, on average, one additional unit will remain vacant for each \$10 increase in rent. What rent should the manager charge to maximize revenue?
7. Find the most general antiderivative of the function. (Check you answer by differentiation.)

$$f(x) = \frac{2 + x^2}{1 + x^2}$$

8. Two balls are thrown upward from the edge of the cliff 432 ft above the ground. The first is thrown at a speed of 48 ft/s and the other is thrown a second later with a speed of 24 ft/s. Do the balls ever pass each other?

9. (a) Batman was driving the Batmobile at 90 mph ( $=132$  ft/sec), when he sees a brick wall directly ahead. When the Batmobile is 400 ft from the wall, he slams on the brakes, decelerating at a constant rate of  $22$  ft/s<sup>2</sup>. Does he stop before he hits the brick wall? If so, how many feet to spare? If not, what is his impact speed?
- (b) Now the Joker had been driving next to Batman, also at 90 mph. But the Joker did not hit his brakes as soon as Batman, continuing for 1 second longer than Batman before hitting his brakes, decelerating at a constant rate of  $22$  ft/s<sup>2</sup>. How fast is he going when he hits the wall? (Don't worry about Joker - he jettisoned at the last instant, to fight for another day!)