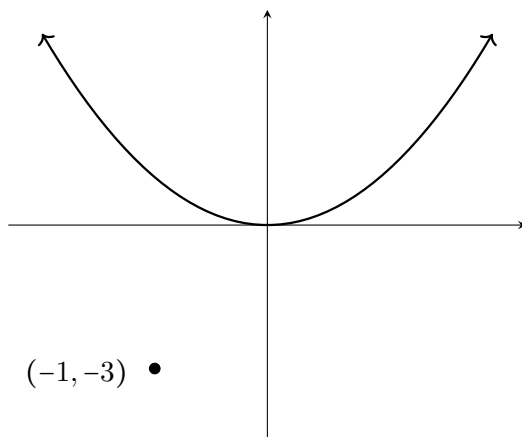


Turn in the following problems:

1. Find equations for the two distinct tangent lines to the curve $y = x^2$ through the point $(-1, -3)$.

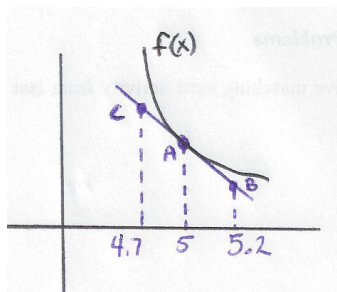


2. Sketch the graph of a function that satisfies all of the given conditions.

- $f'(2) = f'(-2) = 0$
- $f'(x) < 0$ if $|x| < 2$
- $f'(x) > 0$ if $2 < |x| < 3$
- $f'(x) = -1$ if $|x| > 3$
- $f''(x) < 0$ if $-2 < x < 0$
- inflection point $(0, -2)$

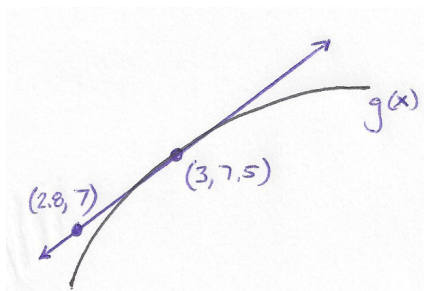
It can be helpful from time to time to sketch a graph or picture to strengthen our understanding of concepts and ideas. Use the following sketches of functions and tangent lines to answer problems below.

3. A sketch of the function $f(x)$ is given below:



If $f(5) = 12$ and $f'(5) = 2$, then find the coordinates of A , B , and C .

4. A sketch of the function $g(x)$ is given below:



If possible, find each of the following. Write “Not enough information” where appropriate.

- (a) $g(3) =$
- (b) $g(2.8) =$
- (c) $g^{-1}(7) =$
- (d) $g'(3) =$
- (e) $g'(2.8) =$

5. The equation $y'' + y' - 2y = x^2$ is called a **differential equation** because it involves an unknown function y and its derivatives y' and y'' . Find constants A , B , and C such that the function $y = Ax^2 + Bx + C$ satisfies this equation. (Differential equations will be studied in detail in Calculus 2).
6. Consider the following mathematical statements. Determine if the statements are always true, sometimes true, or never true.
- (a) If $f''(x) > 0$ on the interval (a, b) , then $f'(x) < 0$ on the interval (a, b) .
 - (b) If $f(x)$ is a polynomial, then it is differentiable for all x .
 - (c) The tangent line to $f(x)$ at $x = a$ will intersect the graph of $f(x)$ at one point.

In mathematics, we consider a statement to be false if we can find any examples where the statement is not true. We refer to these examples as counterexamples. Note that a counterexample is an example for which the “if” part of the statement is true, but the “then” part of the statement is false.

With this in mind, now determine if the above statements are true or false. If the statement is true, give a brief explanation of why it is true. If the statement is false, give a counterexample. Be sure to explain why your counterexample shows the statement to be false.

Optional Challenge Problems

Find a possible formula for each function in the derivative matching card activity from last week (see the “Activities” page of the course website).