

1. Write each sum in series notation, assuming the pattern continues infinitely.

(a) $1 + \frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \dots$

(b) $10 - 2 + 0.4 - 0.08 + \dots$

(c) $0.999\dots = 0.9 + 0.09 + 0.009 + \dots$

2. For each series below, write at least five terms of the sequence of partial sums and the general term if possible. Use the sequence of partial sums to speculate/determine whether the series converges or diverges.

(a) $\sum_{n=1}^{\infty} \left(\frac{1}{n} - \frac{1}{n+1} \right)$

(b) $\sum_{n=0}^{\infty} n$

(c) $\sum_{n=0}^{\infty} \frac{3}{10^n}$

(d) $\sum_{n=1}^{\infty} \frac{1}{n}$

Hint: Use technology to calculate the partial sums with 2, 4, 8, 16, ... terms.

(e) $\sum_{n=0}^{\infty} (-1)^n$

(f) $\sum_{n=1}^{\infty} \ln(n)$

3. For which of the series above do the terms of the series go to zero? Is this related to whether or not the series converges? If so, how?