

1. Prove that if  $F$  is an injective sheaf of abelian groups on  $X$  then  $F$  is flasque.
2. Prove that if  $F'$  is a flasque sheaf of abelian groups and

$$0 \rightarrow F' \rightarrow F \rightarrow F'' \rightarrow 0$$

is exact then  $F$  is flasque if and only if  $F''$  is flasque.

3. Suppose  $X$  is a topological space and  $j : U \rightarrow X$  is the inclusion of an open subset. For any sheaf of abelian groups  $F$  on  $U$ , let  $j_!F = (F^{\text{ét}} \cup_{\{0\} \times U} \{0\} \times X)^{\text{sh}}$ .
  - (a) Show that  $j_!F$  has the structure of a sheaf of abelian groups.
  - (b) Show that  $j_!$  is left adjoint to  $j^{-1}$ .
  - (c) Show that  $j_!(-)$  is an exact functor.
  - (d) Conclude that  $j^{-1}$  preserves injectives when  $j$  is the inclusion of an open subset.