

Problem 1. How long did you spend on this assignment?

- A) < 1 hour
- B) Between 1 and 2 hours
- C) Between 2 and 3 hours
- D) Between 3 and 4 hours
- E) > 4 hours

When it makes sense to do so, answer ‘C’ for “Both” and ‘D’ for “Neither”. You will receive 1/4 point for any question on which you answer ‘E’ for “I don’t know”.

Problem 2. Let S and T be sets. Which of the following is equivalent to $S = T$?

- A) $\forall x, (x \in S \iff x \in T)$
- B) $\exists x, (x \in S \iff x \in T)$

Solution. A) □

Problem 3. The sentences $Y \wedge Z$ and $\forall x \in \{Y, Z\}, x$ are equivalent.

- A) True
- B) False

Solution. A) □

Problem 4. Which of the following sentences are true?

- A) $\forall x \in \mathbb{Z}, \exists y \in \mathbb{Z}, y > x$
- B) $\exists x \in \mathbb{Z}, \forall y \in \mathbb{Z}, y > x$

Solution. A) □

Problem 5. Which of the following sentences are true?

- A) $\forall x, \left((x \text{ lives in Los Angeles}) \implies (x \text{ lives in California}) \right)$
- B) $(\forall x, (x \text{ lives in Los Angeles})) \implies (\forall x, (x \text{ lives in California}))$

Solution. C) □

Problem 6. In this problem $P(x, y)$ is a sentence involving variables x and y . Which of the following is the logical opposite of $\forall x, \exists y, P(x, y)$?

- A) $\forall x, \exists y, \text{not } P(x, y)$
- B) $\exists x, \forall y, \text{not } P(x, y)$

Solution. B) □