

Problem 1. Consider the sentence “Let $x = 6$. Then $y = 7$ is greater than 6.” Which of the following facts does this sentence demonstrate?

- A) It proves “For any integer x there is an integer y with $y > x$.”
- B) It disproves “There is no integer x such that there is an integer y with $y > x$.”
- C) Both
- D) Neither

Solution. B) □

Problem 2. The only way to disprove a statement “ X implies Y ” is to show that there is some situation in which X is true and Y is false.

- A) True
- B) False

Solution. A) □

Problem 3. Let’s agree to call a number *threeven* if it is divisible by 3. How would you disprove the statement “Every number is even or threeven.”

- A) Find a number that is neither even nor threeven

- B) Find a number that is both even and threeven
- C) Find one number that is not even and one number that is not threeven

Solution. A) □

Problem 4. Let’s say that a number is *fourven* if it is divisible by 4. Which of the following sentences is true?

- A) A number that is even is also fourven.
- B) A number that is fourven is also even.
- C) Both.
- D) Neither.

Solution. B) □