

Problem 1. Let A and B be finite sets. How many functions are there from A to B ?

- A) $|A| + |B|$ B) $|A| \times |B|$ C) $|B|^{|A|}$ D) $|A|^{|B|}$ E) None of these

Problem 2. If A and B are *non-empty* sets then there is an injection from A to B if and only if there is a surjection from B to A .

- A) True B) False

Problem 3. Which set is larger?

- A) \mathbf{N} B) \mathbf{Z} C) They are the same size D) The question doesn't make sense

Problem 4. Which set is larger?

- A) \mathbf{N} B) $\mathbf{N} \times \mathbf{N}$ C) They are the same size D) The question doesn't make sense

Problem 5. Let A be a set and recall that 2^A is the set of all subsets of A . Suppose $f : A \rightarrow 2^A$ is a function. Which of the following are possible?

- A) f is injective
B) f is surjective
C) Both of the above (f is bijective)
D) None of the above

Problem 6. Which set is larger?

- A) \mathbf{N} B) \mathbf{R} C) They are the same size D) The question doesn't make sense

Problem 7. Let S be the set of equivalence classes of integers modulo 7 and let

$$f : S \rightarrow S$$

be the function $f([n]) = [n + 3]$. Is this function a permutation?

- A) Yes B) No

Problem 8. Every permutation of a finite set can be written as a composition of transpositions.

- A) Yes B) No

Problem 9. Let A and B be finite sets. How many *bijections* are there from A to B ?

- A) $|B|^{|A|}$ B) $|A|^{|B|}$ C) $|A|!$ D) $|B|!$ E) None of these

Problem 10. Which of the following are true?

- A) The composition of two injections is an injection.
B) The composition of two surjections is a surjection.
C) Both of the above
D) None of the above