

Problem 1. Is $\{\{1\}, \{2, 3\}, \{5\}\}$ a partition?

- A) Yes B) No C) Of what?

Problem 2. How many partitions are there of the empty set?

- A) 0 B) 1 C) ∞ D) The answer is not defined.

Problem 3. How many distinct rearrangements are there of the letters of my name, JONATHAN?

- A) 1 B) 8 C) $2 \times 7!$ D) $8!$ E) None of these

Problem 4. Let n be a positive integer. Compute

$$\sum_{k=0}^n (-1)^k \binom{n}{k} = \binom{n}{0} - \binom{n}{1} + \binom{n}{2} - \cdots + (-1)^n \binom{n}{n}.$$

- A) $\binom{n}{n/2}$ B) $-\binom{n}{n/2}$ C) 0 D) Depends on n .

Problem 5. Let S be a finite set. Which is greater?

- A) The number of partitions of S .
B) The number of equivalence relations on S .
C) They are equal.
D) The answer depends on S .

Problem 6. Let S be a set with n elements. How many ways are there to partition S into *two* subsets.

- A) 1 B) n C) $2^n - 2$ D) 2^n E) None of these

Problem 7. Let S be a set with n elements and let a , b , and c be three positive integers with $a + b + c = n$. You may assume that a , b , and c are all different numbers. Devise a formula using addition, subtraction, multiplication, division, exponentiation, and the factorial for the number of partitions of S into three subsets of sizes a , b , and c .

Problem 8. How does your formula from the last problem change when $a = b \neq c$? What about when $a = b = c$?