Name: ANSWER KEY Score:

1. What is the difference between a sequence and a series?

A sequence is a list of numbers, and a series is the sum of a list of numbers.

2. Does the following geometric series converge? If it does, find its value.

(a)
$$2 + \frac{2}{3} + \frac{2}{9} + \frac{2}{27} + \cdots$$

We can recognize that this is a geometric series because we multiply by $\frac{1}{3}$ to get each new term. In other words, $r = \frac{1}{3}$. Since |r| < 1, the series converges. It converges to $\boxed{\frac{2}{1-\frac{1}{3}} = 3}$

(b) $\sum_{n=1}^{\infty} \left(\frac{\pi}{e}\right)^n$

This geometric series has $r = \frac{\pi}{e}$. Since $\pi > e$, we know $|r| = \frac{\pi}{e} > 1$. Thus this geometric series diverges.

