Exercise 1.1.16

Linear Algebra MATH 2130

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ABSTRACT. This is Exercise 1.1.16 from Lay [LLM16, §1.1]:

Exercise 1.1.16. Determine if the system of equations is consistent. You do not need to completely solve the system of equations.

Solution. The augmented matrix associated to the system of equations is

1	0	3	0	2
0	1	0	-3	3
0	-2	3	2	1
3	0	0	7	-5

We can put the left hand side of the matrix in Row Echelon Form (REF) to determine if the system is consistent. To this aim, adding -3 times the first row to the last row we have

1	0	3	0	2
0	1	0	-3	3
0	-2	3	2	1
0	0	-3	7	-11

Date: August 28, 2022.

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Then adding 2 times the second row to the third row we have

$$\begin{bmatrix} 1 & 0 & 3 & 0 & 2 \\ 0 & 1 & 0 & -3 & 3 \\ 0 & 0 & 3 & -4 & 7 \\ 0 & 0 & -3 & 7 & -11 \end{bmatrix}$$

Finally, adding the third row to the fourth row, we have

1	0	3	0	2
0	1	0	-3	3
0	0	3	-4	7
0	0	0	3	-4

The left hand side is in REF. Since there are no zero rows on the left hand side with non-zero entries on the right, the system is consisent.

References

[LLM16] David Lay, Stephen Lay, and Judi McDonald, Linear Algebra and its Applications, Fifth edition, Pearson, 2016.

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