

MATH 2400: Calculus III, Fall 2013
MIDTERM #3

November 13, 2013

YOUR NAME:

Circle Your CORRECT Section

- 001 E. ANGEL (9AM)
- 002 E. ANGEL (10AM)
- 003 A. NITA (11AM)
- 004 K. SELKER (12PM)
- 005 I. MISHEV (1PM)
- 006 C. FARSI (2PM)
- 007 R. ROSENBAUM (3PM)
- 008 S. HENRY (9AM)

Important note: SHOW ALL WORK. BOX YOUR ANSWERS. Calculators are not allowed. No books, notes, etc. Throughout this exam, please provide exact answers where possible. That is: if the answer is $1/2$, do not write 0.499 or something of that sort; if the answer is π , do not write 3.14159.

Problem	Points	Score
1	25	
2	25	
3	25	
4	25	
TOTAL	100	

“On my honor, as a University of Colorado at Boulder student, I have neither given nor received unauthorized assistance on this work.”

SIGNATURE:

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1. (25 points) Let W be the three-dimensional solid that is bounded below by the cone $z = \sqrt{\frac{x^2 + y^2}{3}}$ and bounded above by the sphere $x^2 + y^2 + z^2 = 9$. Evaluate the following integral

$$\iiint_W e^{(x^2+y^2+z^2)^{3/2}} dx dy dz.$$

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2. (25 points) Use the change of variables $s = y$, $t = y - x^3$ to evaluate $\iint_R x^2 dx dy$ over the region R bounded by $y = 2$, $y = 8$, $y = x^3$, and $y = x^3 + 8$.

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3. Let

$$\vec{F}(x, y) = (3x)\vec{i} + (-3y)\vec{j}.$$

- (a) **(15 points)** Find a parametrization for the flow line of \vec{F} that passes through the point $(1, 3)$.

- (b) **(10 points)** Write Cartesian equations for the flow lines of the vector field $\vec{F}(x, y)$. Cartesian equations are equations involving the standard calculus variables x and y , as well as constants.

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4. Consider the vector field

$$\vec{F}(x, y) = 4[(1 + x^2y^2)xy^2] \vec{i} + 4[(1 + x^2y^2)x^2y + 1] \vec{j}$$

- (a) **(10 points)** Let C be the segment of the hyperbola $y = \frac{1}{x}$ from $(1, 1)$ to $(2, 1/2)$. Evaluate the line integral

$$\int_C \vec{F} \cdot d\vec{r}$$

by parametrizing C . Do **not** use the Fundamental Theorem of Calculus for Line Integrals.

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- (b) **(10 points)** Show that \vec{F} is a conservative vector field by finding a potential function f for \vec{F} : this means finding a function f such that $\nabla f = \vec{F}$.

$$f(x, y) = \underline{\hspace{10em}}.$$

- (c) **(5 points)** Use the Fundamental Theorem of Calculus for Line Integrals to evaluate $\int_C \vec{F} \cdot d\vec{r}$, where C is the segment of the hyperbola $y = \frac{1}{x}$ from $(1, 1)$ to $(2, 1/2)$ given in part (a).